

Widcombe-in-the-Moor Primary School: Number & Calculation policy: Years 3 & 4



Rationale

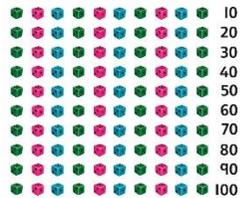
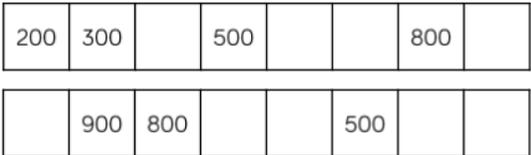
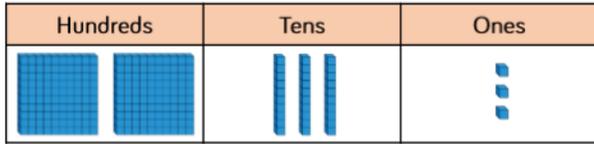
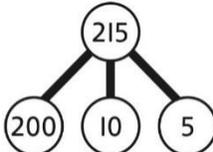
It is our intent to provide children with clear methods and strategies in order to build secure foundations in calculation. In Years 3 & 4 children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding.

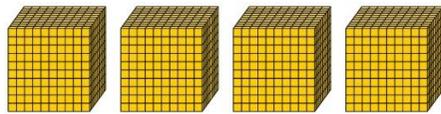
Staff will begin units of work with an elicitation task. These tasks will include questions; (2 of each) fluency, reasoning and problem solving being at the heart of these tasks. These tasks will provide staff with a clear picture of children's knowledge and skills and then allow staff to meet need and extend children's learning from their individual starting points. They will be used again at the end of a unit of work, enabling staff to see a clear picture of progress and mastery of given areas.

Key Vocabulary:

rounding, partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Years 3 & 4

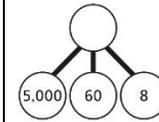
	Concrete	Pictorial	Abstract
Place value	All children will be taught:		
Understanding 100s	<p>Understand the cardinality of 100, and the link with 10 tens.</p> <p>Use cubes to place into groups of 10 tens.</p> 	<p>count in steps of 100.</p> <p>There are 100 sweets in each jar.</p> 	<p>Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.</p> 
Understanding place value to 1,000	<p>Unitise 100s, 10s and 1s to build 3-digit numbers.</p> 	<p>Use equipment to represent numbers to 1,000.</p> 	<p>Represent the parts of numbers to 1,000 using a part-whole model.</p>  <p>$215 = 200 + 10 + 5$</p> <p>Recognise numbers to 1,000 represented on a number line, including those between intervals.</p>
Understanding numbers to 10,000	<p>Use place value equipment to understand the place value of 4-digit numbers.</p>	<p>Represent numbers using place value counters once children understand the relationship between 1,000s and 100s.</p>	<p>Understand partitioning of 4-digit numbers, including numbers with digits of 0.</p>



4 thousands equal 4,000.

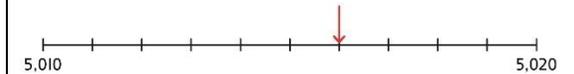


$$4,000 + 300 + 50 + 5 = 4,355$$



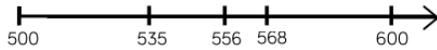
$$5,000 + 60 + 8 = 5,068$$

Understand and read 4-digit numbers on a number line.



Round to the nearest 10/100/1000

Say whether each number on the number line is closer to 500 or 600



Round 535, 556 and 568 to the nearest 100
Use the stem sentence: ____ rounded to the nearest 100 is ____.

Complete the table:

Start number	Rounded to the nearest 10
851	
XCVIII	

Round these numbers to the nearest 1,000

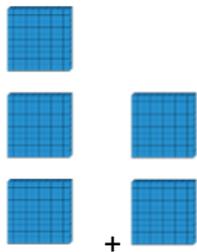
- Eight thousand and fifty-six
- 5 thousands, 5 hundreds, 5 tens and 5 ones
-
- LXXXII

Complete the table.

Start number	Rounded to the nearest 10	Rounded to the nearest 100	Rounded to the nearest 1,000
4,999			
LXXXII			

Adding 100s

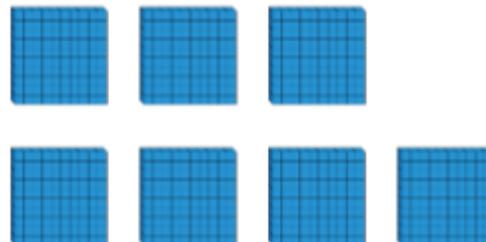
Use known facts and unitising to add multiples of 100.



$$3 + 2 = 5$$

3 hundreds + 2 hundreds = 5 hundreds
300 + 200 = 500

Use known facts and unitising to add multiples of 100.



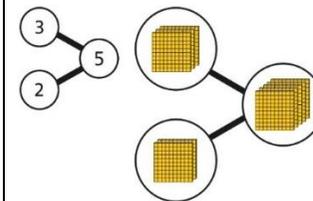
$$3 + 4 = 7$$

3 hundreds + 4 hundreds = 7 hundreds

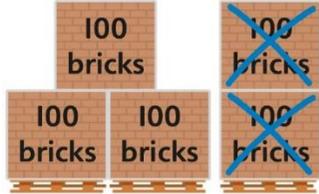
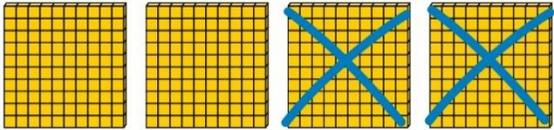
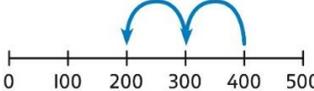
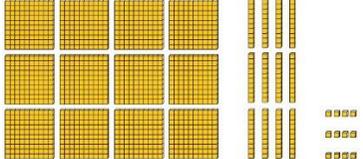
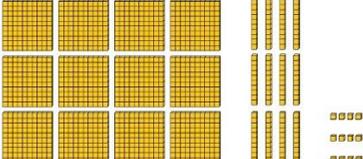
Use known facts and unitising to add multiples of 100.

Represent the addition on a number line.

Use a part-whole model to support unitising.



$$3 + 2 = 5$$

		$300 + 400 = 700$	$300 + 200 = 500$
Subtracting 100s	<p>Use known facts and unitising to subtract multiples of 100.</p>  <p>$5 - 2 = 3$ $500 - 200 = 300$</p>	<p>Use known facts and unitising to subtract multiples of 100.</p>  <p>$4 - 2 = 2$ $400 - 200 = 200$</p>	<p>Understand the link with counting back in 100s.</p>  <p>$400 - 200 = 200$</p> <p>Use known facts and unitising as efficient and accurate methods. I know that $7 - 4 = 3$. Therefore, I know that $700 - 400 = 300$.</p>
Multiplying by multiples of 10 and 100	<p>Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.</p>  <p>3 groups of 4 ones is 12 ones. 3 groups of 4 tens is 12 tens. 3 groups of 4 hundreds is 12 hundreds.</p>	<p>Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.</p>  <p>$3 \times 4 = 12$ $3 \times 40 = 120$ $3 \times 400 = 1,200$</p>	<p>Use known facts and understanding of place value and commutativity to multiply mentally.</p> <p>$4 \times 7 = 28$</p> <p>$4 \times 70 = 280$ $40 \times 7 = 280$</p> <p>$4 \times 700 = 2,800$ $400 \times 7 = 2,800$</p>
Addition	<p>All children will be taught the column method. Place value equipment will be used to represent additions and support mathematics where necessary. Other methods may also offer support to secure knowledge and skills. All children will be taught to add 1/10/100 without exchange and then add 1/10/100 with exchange</p>		
	Concrete	Pictorial	Abstract
3 / 4-digit number + 1s, no exchange or bridging	Use number bonds to add the 1s.	Use number bonds to add the 1s.	Understand the link with counting on. $245 + 4$



$$214 + 4 = ?$$

Now there are 4 + 4 ones in total.

$$4 + 4 = 8$$

$$214 + 4 = 218$$

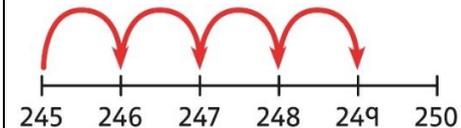
H	T	O
2	4	9

Use number bonds to add the 1s.
5 + 4 = 9

$$245 + 4$$

$$5 + 4 = 9$$

$$245 + 4 = 249$$



Use number bonds to add the 1s and understand that this is more efficient and less prone to error.

$$245 + 4 = ?$$

I will add the 1s.

$$5 + 4 = 9$$

$$\text{So, } 245 + 4 = 249$$

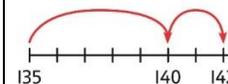
3 / 4-digit number + 1s with exchange

Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.

Children should explore this using unitised objects or physical apparatus.

Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.

Understand how to bridge by partitioning to the 1s to make the next 10.



$$135 + 7 = ?$$

$135 + 5 + 2 = 142$ Ensure that children understand how to add 1s bridging a 100.

$$198 + 5 = ?$$

$$198 + 2 + 3 = 203$$

3-digit number + 10s, no exchange

Calculate mentally by forming the number bond for the 10s.

Calculate mentally by forming the number bond for the 10s.

$$98 + 4142 = \text{[blue box]}$$

make 100

$$98 + 4142 = 100 + 4140 = 4240$$

Calculate mentally by forming the number bond for the 10s.

$$753 + 40$$

I know that 5 + 4 = 9

$$\text{So, } 50 + 40 = 90$$

$$753 + 40 = 793$$

Add 9 to 3041.

$$3041 + 9 = \square$$

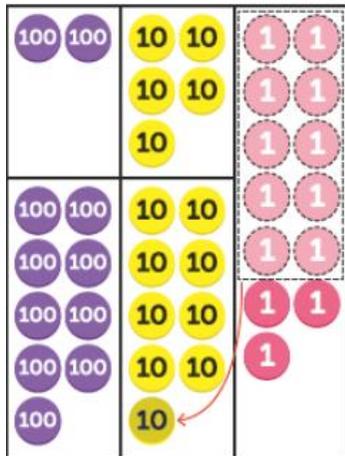
make 10

$$3041 + 9 = 3040 + 10$$

$$3041 + 9 = 3050$$

3-digit number + 2-digit / 3 digit number, exchange required

Use place value equipment / grids to model addition and understand where exchange is required.



There are 13 ones, so that is 1 ten and 3 ones. There are 14 tens so I will exchange.

Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation.

$$\begin{array}{r} \text{H T O} \\ 275 \\ + 16 \\ \hline \end{array}$$

$$\begin{array}{r} \text{H T O} \\ 275 \\ + 16 \\ \hline 91 \end{array}$$

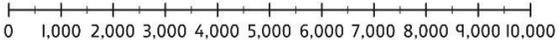
$$\begin{array}{r} \text{H T O} \\ 275 \\ + 16 \\ \hline 291 \end{array}$$

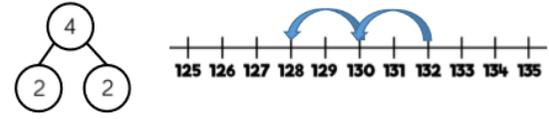
$$275 + 16 = 291$$

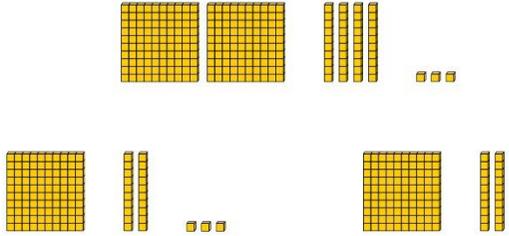
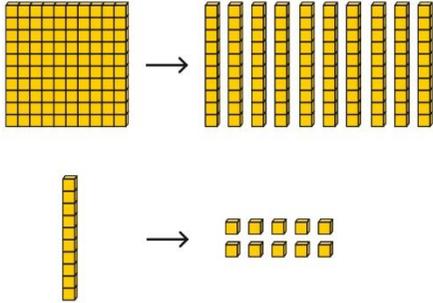
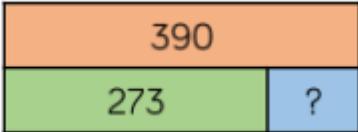
Representing additions and checking strategies

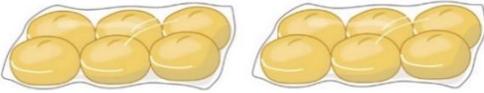
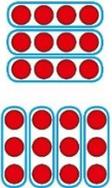
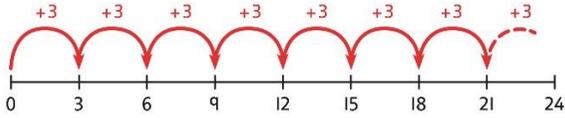
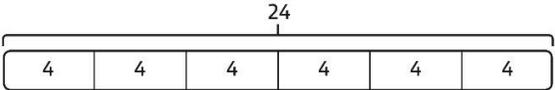
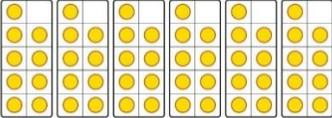
Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate.

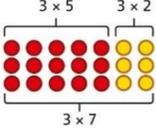
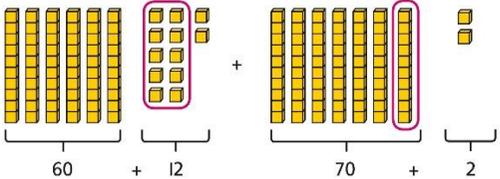
Use rounding and estimating on a number line to check the reasonableness of an addition.

		<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td colspan="2" style="text-align: center;">1,373</td></tr> <tr><td style="text-align: center;">799</td><td style="text-align: center;">574</td></tr> </table> <div style="margin-left: 100px;"> <table style="border-collapse: collapse;"> <tr><td style="padding: 0 5px;">Th</td><td style="padding: 0 5px;">H</td><td style="padding: 0 5px;">T</td><td style="padding: 0 5px;">O</td></tr> <tr><td style="text-align: center;">7</td><td style="text-align: center;">9</td><td style="text-align: center;">9</td><td></td></tr> <tr><td colspan="4" style="text-align: center;">+</td></tr> <tr><td style="text-align: center;">1</td><td style="text-align: center;">3</td><td style="text-align: center;">7</td><td style="text-align: center;">3</td></tr> <tr><td colspan="4" style="text-align: center;">-----</td></tr> <tr><td></td><td></td><td></td><td></td></tr> </table> </div> <p style="margin-left: 100px;"><i>I chose to work out 574 + 800, then subtract 1.</i></p>	1,373		799	574	Th	H	T	O	7	9	9		+				1	3	7	3	-----								 <p>$912 + 6,149 = ?$</p> <p><i>I used rounding to work out that the answer should be approximately $1,000 + 6,000 = 7,000$.</i></p>
1,373																															
799	574																														
Th	H	T	O																												
7	9	9																													
+																															
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Subtraction	All children will be taught column subtraction. Place value equipment will be used to represent subtractions and support mathematics where necessary. Other methods may also offer support to secure knowledge and skills. All children will be taught to subtract without exchange and then subtract with exchange																														
	Concrete	Pictorial	Abstract																												
3-digit number – 1s, no exchange	<p>Use number bonds to subtract the 1s.</p>  <p>$214 - 3 = ?$</p>  <p>$4 - 3 = 1$ $214 - 3 = 211$</p>	<p>Use number bonds to subtract the 1s.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;">H</td><td style="text-align: center;">T</td><td style="text-align: center;">O</td></tr> <tr><td style="text-align: center;">3</td><td style="text-align: center;">1</td><td style="text-align: center;">9</td></tr> </table> <p>$319 - 4 = ?$</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;">H</td><td style="text-align: center;">T</td><td style="text-align: center;">O</td></tr> <tr><td style="text-align: center;">3</td><td style="text-align: center;">1</td><td style="text-align: center;">9</td></tr> </table> <p>$9 - 4 = 5$ $319 - 4 = 315$</p>	H	T	O	3	1	9	H	T	O	3	1	9	<p>Understand the link with counting back using a number line.</p> <p>$132 - 4$</p> 																
H	T	O																													
3	1	9																													
H	T	O																													
3	1	9																													
3-digit number – up to 3 / 4-digit number	<p>Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.</p>	<p>Represent the calculation on a place value grid.</p> 	<p>Use column subtraction to calculate accurately and efficiently.</p>																												

			$\begin{array}{r} \text{H T O} \\ 999 \\ - 352 \\ \hline 7 \end{array}$ $\begin{array}{r} \text{H T O} \\ 999 \\ - 352 \\ \hline 47 \end{array}$ $\begin{array}{r} \text{H T O} \\ 999 \\ - 352 \\ \hline 647 \end{array}$
<p>3-digit number – up to 3-digit number, exchange required</p>	<p>Use equipment to exchange 1 hundred for 10 tens, and 1 ten for 10 ones.</p> 	<p><i>Model the required exchange on a place value grid.</i></p> <p>$175 - 38 = ?$ <i>I need to subtract 8 ones, so I will exchange a ten for 10 ones.</i></p>	<p>Use column subtraction to work accurately and efficiently.</p> $\begin{array}{r} \text{H T O} \\ 175 \\ - 38 \\ \hline 137 \end{array}$ <p>$175 - 38 = 137$</p>
<p>Representing subtraction problems</p>		<p>Use bar models to represent subtractions.</p> <p>‘Find the difference’ is represented as two bars for comparison.</p>  <p>Bar models can also be used to show that a part must be taken away from the whole.</p>	<p>Children use alternative representations to check calculations and choose efficient methods.</p> <p>Children use inverse operations to check additions and subtractions.</p> $\begin{array}{r} \text{H T O} \\ 270 \\ + 255 \\ \hline 525 \end{array}$ <p>I will check using addition.</p>

Multiplication			
All children will be taught times tables to 12x12 and begin with formal written methods for short multiplication			
	Concrete	Pictorial	Abstract
<p>Understanding equal grouping and repeated addition</p> <p>Using commutativity to support understanding of the times-tables</p>	<p>Children continue to build understanding of equal groups and the relationship with repeated addition.</p>  <p>Children recognise that arrays can be used to model commutative multiplications.</p>  <p><i>I can see 2 groups of 6. I can see 6 groups of 2. $2 \times 6 = 12$ $6 \times 2 = 12$</i></p>	<p>Children recognise that arrays demonstrate commutativity.</p>  <p><i>This is 3 groups of 4. This is 4 groups of 3.</i></p> <p>$3 \times 4 = 12$ $4 \times 3 = 12$</p>	<p>Children understand the link between repeated addition and multiplication.</p>  <p><i>8 groups of 3 is 24.</i></p> <p>$3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 24$ $8 \times 3 = 24$</p> <p>A bar model may represent multiplications as equal groups.</p>  <p>$6 \times 4 = 24$</p>
<p>Learning and understanding times-tables up to 12 x 12</p>	<p>Learn times tables to 12x12</p> <p>Understand the special cases of multiplying by 1 and 0.</p>  <p>$5 \times 1 = 5$</p>  <p>$5 \times 0 = 0$</p>	<p>Represent the relationship between the x9 table and the x10 table.</p>  <p>Represent the x11 table and x12 tables in relation to the x10 table.</p>	<p>Understand how times-tables relate to counting patterns.</p> <p>Understand links between the x3 table, x6 table and x9 table <i>5 x 6 is double 5 x 3</i></p> <p>x5 table and x6 table <i>I know that $7 \times 5 = 35$ so I know that $7 \times 6 = 35 + 7$.</i></p>

		 $2 \times 11 = 20 + 2$ $3 \times 11 = 30 + 3$ $4 \times 11 = 40 + 4$  $4 \times 12 = 40 + 8$	<p>x5 table and x7 table</p> $3 \times 7 = 3 \times 5 + 3 \times 2$  <p>x9 table and x10 table</p> $6 \times 10 = 60$ $6 \times 9 = 60 - 6$												
<p>Multiplying a 2-digit number by a 1-digit number, expanded column method</p>	<p>Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications.</p> $3 \times 24 = ?$ $3 \times 20 = 60$ $3 \times 4 = 12$  $3 \times 24 = 60 + 12$ $3 \times 24 = 70 + 2$ $3 \times 24 = 72$	<p>Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s.</p> $4 \times 23 = ?$ $4 \times 20 = 80$ $4 \times 3 = 12$ $4 \times 23 = 92$	<p>Short multiplication method</p> <table border="1" data-bbox="1559 579 1722 802"> <tbody> <tr> <td></td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td>3</td> <td>4</td> </tr> <tr> <td>x</td> <td></td> <td>5</td> </tr> <tr> <td>1</td> <td>7</td> <td>0</td> </tr> </tbody> </table> <p>1 2</p>		T	O		3	4	x		5	1	7	0
	T	O													
	3	4													
x		5													
1	7	0													
<p>Column multiplication for 2- and 3-digit numbers multiplied by a single digit</p>	<p>Use place value equipment to make multiplications. 26×3</p>	<p>Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit.</p>	<p>Use the formal column method for up to 3-digit numbers multiplied by a single digit.</p> $\begin{array}{r} 312 \\ \times 3 \\ \hline 936 \end{array}$												

Tens	Ones

There are 3×6 ones... 18 ones
 There are 3×2 tens ... 6 tens
 $18 + 60 = 78$

Tens	Ones

	T	O
	3	4
x		2
	6	8

Division

All children will be taught short division method (bus stop)

Concrete

Use objects to explore families of multiplication and division facts.



$12 \div 3 = 4$ $3 = 12 \div 4$
 $12 = 4 \times 3$ $3 \times 12 = 4$
 $3 \div 4 = 12$ $3 \times 4 = 12$

Understanding the relationship between multiplication and division, including times-tables

Concrete

Represent divisions using an array.



$24 \div 4 = 6$

Concrete

Understand families of related multiplication and division facts.

I know that $5 \times 7 = 35$

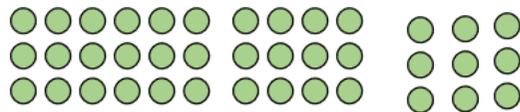
so I know all these facts:

- $5 \times 7 = 35$
- $7 \times 5 = 35$
- $35 = 5 \times 7$
- $35 = 7 \times 5$
- $35 \div 5 = 7$
- $35 \div 7 = 5$
- $7 = 35 \div 5$
- $5 = 35 \div 7$

Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s

Partition into 10s and 1s to divide where appropriate.

$39 \div 3 = ?$



$39 = 30 + 9$

Partition into 100s, 10s and 1s using a part-whole model to divide where appropriate.

$142 \div 2 = ?$

$100 \div 2 = \square$ $40 \div 2 = \square$ $6 \div 2 = \square$

$$30 \div 3 = 10$$

$$9 \div 3 = 3$$

$$39 \div 3 = 13$$

Use Base 10 equipment to divide where appropriate.

$$100 \div 2 = 50$$

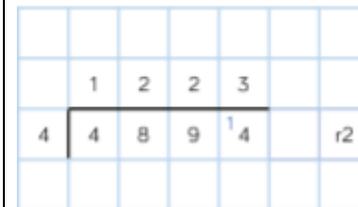
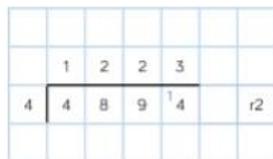
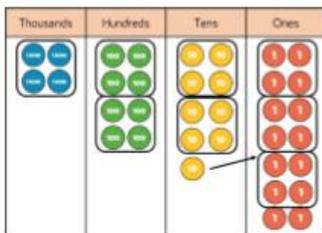
$$40 \div 2 = 20$$

$$6 \div 2 = 3$$

$$50 + 20 + 3 = 73$$

$$142 \div 2 = 71$$

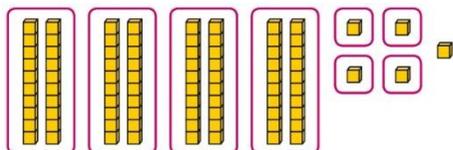
Dividing 2-digit and 3-digit numbers by a single digit, using short division



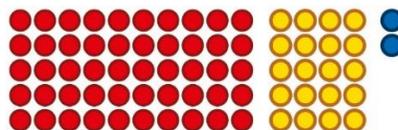
Understanding remainders

Use place value equipment to find remainders.

*85 shared into 4 equal groups
There are 24, and 1 that cannot be shared.*



Represent the remainder as the part that cannot be shared equally.



$$72 \div 5 = 14 \text{ remainder } 2$$

Understand how partitioning can reveal remainders of divisions.

$$80 \div 4 = 20$$

$$12 \div 4 = 3$$

$$95 \div 4 = 23 \text{ remainder } 3$$